

**CONTROL SYSTEMS  
(AEIE 3104)**

Time Allotted : 3 hrs

Full Marks : 70

Figures out of the right margin indicate full marks.

Candidates are required to answer Group A and any 5 (five) from Group B to E, taking at least one from each group.

Candidates are required to give answer in their own words as far as practicable.

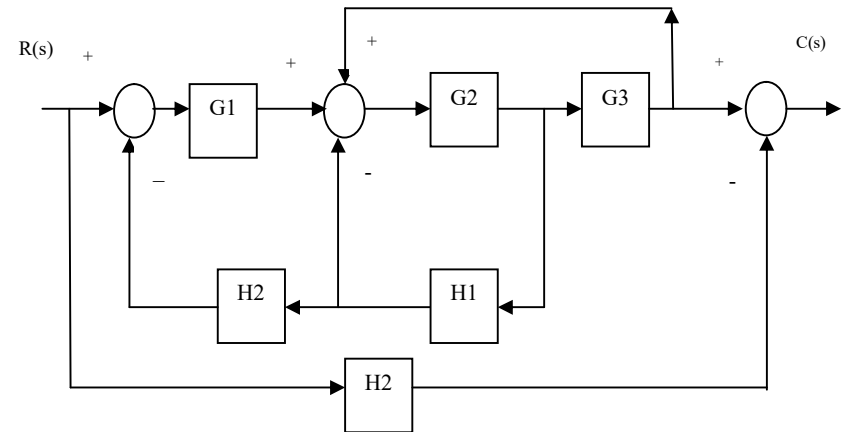
**Group - A  
(Multiple Choice Type Questions)**

1. Choose the correct alternative for the following: 10 × 1 = 10
  - (i) The damping ratio of the second order system  $2d^2y/dt^2 + 4dy/dt + 8y = 8x$  is  
 (a) 0.1                      (b) 0.25                      (c) 1                      (d) 0.5.
  - (ii) If the characteristic equation of a system is  $(s^2 + s + 16) = 0$ , the system is  
 (a) undamped                      (b) underdamped  
 (c) critically damped                      (d) overdamped.
  - (iii) The type of a transfer function denotes the number of  
 (a) zeros at origin                      (b) poles at infinity  
 (c) poles at origin                      (d) none of these.
  - (iv) A system has a simple pole at origin. Its unit impulse response will be  
 (a) ramp                      (b) decaying exponentially  
 (c) oscillatory                      (d) constant.
  - (v) A closed loop system is stable if  
 (a) GM = -ve & PM = +ve                      (b) GM = +ve & PM = +ve  
 (c) GM = -ve & PM = -ve                      (d) GM = +ve & PM = -ve.
  - (vi) A second order system exhibits 100% overshoot. Its damping ratio is  
 (a) 1                      (b) less than 1                      (c) greater than 1                      (d) 0.
  - (vii) For the unit step response of a system having closed loop transfer function  $4 / (s^2 + 8s + 4)$ , the settling time on 2% basis is  
 (a) 1.86 sec                      (b) 4 sec                      (c) 1 sec                      (d) 2.86 sec.

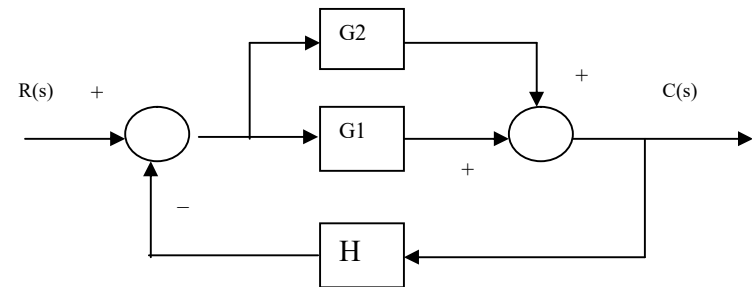
- (viii) The root locus of a system has three asymptotes. The system can have  
 (a) 5 poles and 2 zeros                      (b) 3 poles and 1 zero  
 (c) 4 poles and 2 zeros                      (d) 6 poles and 2 zeros.
- (ix) The Routh-Hurwitz criteria gives  
 (a) absolute stability                      (b) gain margin  
 (c) phase margin                      (d) none of these.
- (x) The phase margin of a system is used to specify  
 (a) frequency response                      (b) absolute stability  
 (c) time response                      (d) relative stability.

**Group - B**

2. (a) Find the overall transfer function of a system having the following block diagram using block reduction technique.



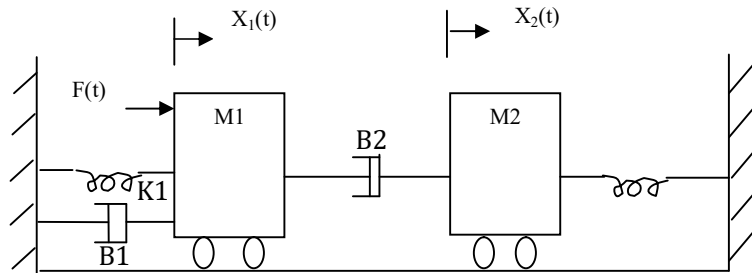
- (b)



Draw the signal flow graph of the above block diagram and find the overall transfer function of the system using Mason's gain formula.

7 + 5 = 12

3. (a)



For the above mechanical system find out  $X_2(s) / F(s)$  considering  $fc_1$  and  $fc_2$  as the frictional coefficients for the mass M1 and M2.

(b) A system matrix A is given by  $A = \begin{bmatrix} -1.8124 & -0.2324 \\ 9.6837 & 1.4697 \end{bmatrix}$   
Find the stability of the system.

7 + 5 = 12

**Group - C**

4. (a) Write a short note on field controlled dc servomotor.  
(b) Derive the expression for the unit step response of a first order negative unity feedback system having open loop transfer function  $G(s) = 1 / sT$ , where T is the time constant of the system. Hence draw the response and find the steady state value.

7 + 5 = 12

5. (a) Derive the expression for the unit step response of a second order negative feedback system having open loop transfer function  $G(s) = \frac{W_n^2}{s(s+2d W_n)}$ , where d is the damping ratio &  $W_n$  is the natural frequency of oscillations.

(b) For the above system find the expression for peak time and maximum percentage peak overshoot.

7 + 5 = 12

**Group - D**

6. (a) For a unity negative feedback system having open loop transfer function  $G(s) = K(s + 1) / [s^3 + as^2 + 2s + 1]$ , determine the values of K and 'a' so that the given system oscillates at a frequency of 4 rad/sec.

- (b) The open loop transfer function of a unity feedback control system is given by  $G(s) = K / [s (sT_1 + 1)(sT_2 + 1)]$ . Find the value of K in terms of  $T_1$  &  $T_2$  so that the system is stable.

7 + 5 = 12

7. For the system having open loop transfer function  $G(s) = K / [s (s + 4) (s^2 + 4s + 13)]$ , sketch the root locus plot by finding out the required parameters. Hence comment on the stability of the above system.

(10 + 2) = 12

**Group - E**

8. (a) Construct the Bode plot for a unity feedback control system having open loop transfer function  $G(s) = 10^7 / [s (s + 10) (s + 1000)]$ .  
(b) From the plot obtain the gain margin, phase margin, gain cross-over frequency and phase cross-over frequency. Hence comment on the stability of the system.

7 + 5 = 12

9. Sketch the Nyquist plot for a unity feedback system having open loop transfer function  $G(s) = 5 / [s(s + 1) (s + 2)]$ . Hence comment on the closed loop stability of the system.

(10 + 2) = 12