

**CODING & INFORMATION THEORY**  
**(ECEN 4102)**

**Time Allotted : 3 hrs**

**Full Marks : 70**

*Figures out of the right margin indicate full marks.*

*Candidates are required to answer Group A and any 5 (five) from Group B to E, taking at least one from each group.*

*Candidates are required to give answer in their own words as far as practicable.*

**Group - A**  
**(Multiple Choice Type Questions)**

1. Choose the correct alternative for the following: **10 × 1 = 10**
- (i) Entropy of a random variable is  
(a) 0            (b) 1            (c) Infinite            (d) Cannot be determined.
  - (ii) Block codes are generated using  
(a) Generator polynomial            (b) Generator matrix  
(c) Generator polynomial & matrix            (d) None of the mentioned.
  - (iii) What are the conjugates of  $\alpha^3$  in GF ( $2^3$ )?  
(a)  $\alpha^6$  and  $\alpha^5$             (b)  $\alpha^5$  and  $\alpha^4$   
(c)  $\alpha^3$  and  $\alpha^4$             (d)  $\alpha^4$  and  $\alpha^6$ .
  - (iv) For a Hamming distance of 5, how many errors can be detected?  
(a) 2            (b) 3            (c) 4            (d) 5.
  - (v) What is the hamming weight for X= 1011101?  
(a) 4            (b) 5            (c) 1            (d) 7.
  - (vi) What is the order of the field element  $\alpha^{12}$  of GF ( $2^4$ )?  
(a) 2            (b) 3            (c) 4            (d) 5.
  - (vii) For decoding in convolution coding, in a code tree,  
(a) Diverge upward when a bit is 0 and diverge downward when the bit is 1  
(b) Diverge downward when a bit is 0 and diverge upward when the bit is 1  
(c) Diverge left when a bit is 0 and diverge right when the bit is 1  
(d) Diverge right when a bit is 0 and diverge left when the bit is 1.

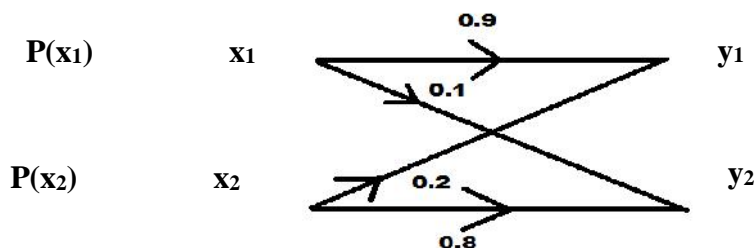
- (viii) A cyclic code can be generated using
  - (a) Generator polynomial
  - (b) Generator matrix
  - (c) Generator polynomial and generator matrix
  - (d) None of the above.
- (ix) Viterbi algorithm performs \_\_\_\_\_ decoding of convolutional codes.
  - (a) Maximum likelihood
  - (b) Maximum a posteriori
  - (c) Minimum square
  - (d) Minimum mean square.
- (x) What will be the amount of information if  $P(x_i) = \frac{1}{4}$ ?
  - (a) 1bit
  - (b) 2bits
  - (c) 3bits
  - (d) 4 bits.

**Group - B**

- 2. (a) Why is Huffman code called an optimum code?
- (b) A DMS has five symbols  $x_1, x_2, x_3, x_4$  and  $x_5$  with  $P(x_1)=0.4, P(x_2)=0.19, P(x_3)=0.16, P(x_4)=0.15$  and  $P(x_5)=0.1$ . Construct a Shanon Fano code for the source and calculate the code efficiency.
- (c) What is conditional entropy?

$3 + (5 + 2) + 2 = 12$

- 3. (a) Given a binary channel shown in the figure.



- i) Find the channel matrix of the channel.
- ii) Find  $P(y_1)$  and  $P(y_2)$  when  $P(x_1) = P(x_2) = 0.5$
- iii) Find the joint probabilities  $P_{(x_1,y_2)}$  and  $P_{(x_2,y_1)}$  when  $P_{(x_1)} = P_{(x_2)} = 0.5$
- (b) An analog signal band limited to 10 kHz is quantized in 8 levels of a PCM system with probabilities  $\frac{1}{4}, \frac{1}{5}, \frac{1}{5}, \frac{1}{10}, \frac{1}{10}, \frac{1}{20}, \frac{1}{20}, \frac{1}{20}$  respectively. Calculate entropy and rate of information.
- (c) For a lossless channel, prove that  $H(X|Y) = 0$ .

$(2+2+2) + (2+2) + 2 = 12$

### Group - C

4. (a) For a Hamming distance of 3, how many errors can be detected? How many errors can be corrected?

(b) Define G and H matrix and show that  $G \cdot H^T = 0$

(c) Parity check matrix of linear block code is

$$H = \left[ \begin{array}{ccc|ccc} 1 & 0 & 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 & 0 & 1 \end{array} \right]$$

(i) Determine the generator matrix

(ii) Assuming that a vector [111011] is received, find the correct data.

$$(2 + 2) + 4 + (2 + 2) = 12$$

5. (a) The parity check bits of a (7,4) block code are generated by

$$C_5 = d_1 \oplus d_2 \oplus d_4; C_6 = d_1 \oplus d_3; C_7 = d_1 \oplus d_3 \oplus d_4$$

(i) Construct the corresponding generator matrix?

(ii) Find the systematic code corresponding to the information bits [1100] and [1010]?

(iii) If the received words are  $v_1 = [1011001]$  and  $v_2 = [1111011]$ ; find the correct code words.

(b) Derive the relation between syndrome S and the error vector E.

$$(3 + 3 + 3) + 3 = 12$$

### Group - D

6. (a) For a systematic (7, 3) cyclic code determine the generator matrix and parity check matrix if  $g(x) = x^4 + x^2 + x + 1$

(b) Code word polynomial  $c(x)$  belonging to the (7, 4) cyclic code with  $g(x) = 1 + x + x^3$  incurs errors so as to produce received polynomial  $v(x)$ .

Find  $c(x)$  when

(i)  $v(x) = x^5 + x^2 + 1$

(ii)  $v(x) = x^6 + x^3 + 1$

$$6 + 6 = 12$$

7. (a) For a (2, 1, 2) convolution code,  $g^0 = (111)$  and  $g^1 = (101)$ . Draw the encoder. Find the state diagram, for this convolution code.

(b) What is constraint length in convolution code?

(c) Consider a received codeword  $r = \underline{11} \underline{11} \underline{10} \underline{01} \underline{10}$  at the instants of time  $j=0,1,2,3,4$  respectively. Find the decoded codeword by applying any decoding scheme.

$$(2 + 3) + 2 + 5 = 12$$

**Group - E**

8. (a) Determine the Galois field elements of  $GF(2^4)$  for the corresponding polynomial  $p(x) = x^4 + x + 1$ .
- (b) What do you mean by primitive element?  $\alpha^{10}, \alpha^7$  are field elements of  $GF(2^4)$ , determine their order and check whether or not they are primitive elements.  
Find the minimal polynomial of  $\alpha^5$  in  $GF(2^3)$ .
- 4 + (1 + 2 + 2) + 3 = 12**
9. Write short notes on (any three)
- (i) Shannon-Fano code
  - (ii) Turbo codes
  - (iii) Hamming code
  - (iv) Source coding
  - (v) Golay code

**(3 × 4) = 12**

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