

# Performance Evaluation of Free Vibration of Laminated Composite Stiffened Hyperbolic Paraboloid Shell Panel with Cutout

Sarmila Sahoo

Department of Civil Engineering, Heritage Institute of Technology, Kolkata 700107, India

E-mail: sarmila.sahoo@gmail.com, sarmila\_ju@yahoo.com

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**Abstract.** The paper considers free vibration characteristics of stiffened composite hyperbolic paraboloid shell panel with cutout in terms of natural frequency and mode shapes. A finite element code is developed for the purpose by combining an eight noded curved shell element with a three noded curved beam element. The size of the cutouts and their positions with respect to the shell centre are varied for different edge conditions of cross-ply and angle-ply laminated shells. The effects of these parametric variations on the fundamental frequencies and mode shapes are considered in details to conclude a set of inferences of practical engineering significance.

## Notations

$a, b$	length and width of shell in plan
$a', b'$	length and width of cutout in plan
$b_{st}$	width of stiffener in general
$b_{sx}, b_{sy}$	width of x and y stiffeners respectively
$B_{sx}, B_{sy}$	strain displacement matrix of stiffener elements
$d_{st}$	depth of stiffener in general
$d_{sx}, d_{sy}$	depth of x and y stiffeners respectively
$\{d_e\}$	element displacement
$e_{sx}, e_{sy}$	eccentricities of x and y -stiffeners with respect to shell mid-surface respectively
$E_{11}, E_{22}$	elastic moduli
$G_{12}, G_{13}, G_{23}$	shear moduli of a lamina with respect to 1, 2 and 3 axes of fibre
$h$	shell thickness
$M_x, M_y$	moment resultants
$M_{xy}$	torsion resultant
$np$	number of plies in a laminate
$N_1-N_8$	shape functions
$N_x, N_y$	inplane force resultants
$N_{xy}$	inplane shear resultant
$Q_x, Q_y$	transverse shear resultant
$R_{xx}, R_{yy}, R_{xy}$	radii of curvature and cross curvature of shell respectively
$u, v, w$	translational degrees of freedom
$x, y, z$	local co-ordinate axes
$X, Y, Z$	global co-ordinate axes
$z_k$	distance of bottom of the kth ply from mid-surface of a laminate
$\alpha, \beta$	rotational degrees of freedom
$\epsilon_x, \epsilon_y$	inplane strain component
$\gamma_{xy}, \gamma_{xz}, \gamma_{yz}$	shearing strain components
$\nu_{12}, \nu_{21}$	Poisson's ratios
$\xi, \eta, \tau$	isoparametric co-ordinates
$\rho$	density of material