

## EM THEORY & TRANSMISSION LINES (ECE2203)

**Time Allotted : 2½ hrs**

**Full Marks : 60**

*Figures out of the right margin indicate full marks.*

*Candidates are required to answer Group A and any 4 (four) from Group B to E, taking one from each group.*

*Candidates are required to give answer in their own words as far as practicable.*

### Group – A

1. Answer any twelve:

**12 × 1 = 12**

*Choose the correct alternative for the following*

- (i) Which equation will hold good for a magnetic material?  
 (a) Line integral of B is zero                      (b) Surface integral of H is zero  
 (c) Line integral of H is zero                      (d) Surface integral of B is zero
- (ii) For a time-harmonic electric field  $\mathbf{E} = E_0 e^{j(\omega t - kz)} \mathbf{a}_y$  in free space, which of the following expressions represents the wave number k?  
 (a)  $k = \omega/c$               (b)  $k = c/\omega$               (c)  $k = \omega/\epsilon_0 \mu_0$               (d)  $k = 1/\sqrt{\epsilon_0 \mu_0}$
- (iii) The flux through each turn of a 100-turn coil is  $(t^3 - 2t)$  mWb, where  $t$  is in seconds. The induced emf at  $t = 2$  s is  
 (a) 1V                      (b) -1V                      (c) 4Mv                      (d) 0.4V
- (iv) Which of the following equations is not Maxwell's equation  
 (a)  $\nabla \cdot \mathbf{J} + \frac{\partial \rho_v}{\partial t} = 0$                       (b)  $\nabla \cdot \mathbf{D} = \rho_v$   
 (c)  $\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$                       (d)  $\oint \mathbf{H} \cdot d\mathbf{l} = \int (\sigma \mathbf{E} + \epsilon \frac{\partial \mathbf{E}}{\partial t}) \cdot d\mathbf{S}$
- (v) If  $\mathbf{E}_s = 10 e^{j4x} \mathbf{a}_y$ , which of the following is incorrect representation of  $\mathbf{E}$ ?  
 (a)  $\text{Re}(\mathbf{E}_s e^{j\omega t})$                       (b)  $\text{Im}(\mathbf{E}_s e^{j\omega t})$   
 (c)  $10 \cos(\omega t + j4x)$                       (d)  $10 \sin(\omega t + 4x)$
- (vi) Given that the reflection coefficient is 0.6. Find the SWR.  
 (a) 2                      (b) 4                      (c) 6                      (d) 8
- (vii) Find the characteristic impedance expression for lossless transmission  
 (a)  $Z_0 = L/C$                       (b)  $Z_0 = \sqrt{L/C}$   
 (c)  $Z_0 = \sqrt{LC}$                       (d)  $Z_0 = LC$
- (viii) The radiation resistance of a Hertzian dipole is typically very small because  
 (a) The dipole is electrically large              (b) The dipole is a short current element  
 (c) It operates at high frequencies              (d) It has a high input impedance

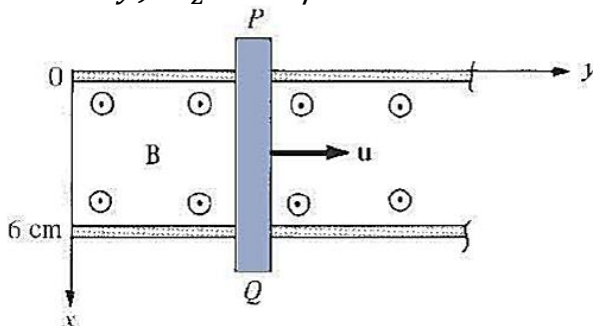
- (ix) The radiation pattern of a Yagi-Uda antenna is  
 (a) Omnidirectional  
 (b) Bidirectional  
 (c) Highly directional with a main lobe in the direction of the director  
 (d) Isotropic
- (x) A linear array of 6 elements is designed to operate at 2.5 GHz with an inter-element spacing of  $0.2\lambda$ . What is the physical distance between the elements in meters?  
 (a) 0.012 m      (b) 0.024 m      (c) 0.036 m      (d) 0.048 m

*Fill in the blanks with the correct word*

- (xi)  $\frac{\partial \mathbf{D}}{\partial t}$  is called as \_\_\_\_\_ current.
- (xii) Two dielectric mediums are characterized by  $\eta_1 = 5$  and  $\eta_2 = 3$ . The reflection coefficient from medium 2 to medium 1 is \_\_\_\_\_.
- (xiii) The condition for a distortionless line is \_\_\_\_\_.
- (xiv) A load impedance of 250 ohm is connected to a 75 ohm line. Reflection coefficient is \_\_\_\_\_.
- (xv) If an antenna array has elements spaced by  $\lambda/2$ , the phase difference required for broadside radiation is \_\_\_\_\_ degrees.

### Group - B

2. (a) Write Maxwell's equations in point form. [[CO1](Remember/LOCQ)]  
 (b) In a charge-free region for which  $\sigma = 0$ ,  $\mu = \mu_0$ , and  $\epsilon = \epsilon_0 \epsilon_r$   
 $\mathbf{H} = 5 \cos(10^{11} t - 4y) \mathbf{a}_z \text{ A/m}$   
 Find: (a)  $\mathbf{J}_d$  and  $\mathbf{D}$ , (b)  $\epsilon_r$  [[CO1](Analyse/IOCQ)]  
 (c) Differentiate between induced EMF and electrostatic potential. [[CO1](Remember/LOCQ)]  
**3 + 7 + 2 = 12**
3. (a) A conducting loop is moving with a velocity  $\mathbf{u}$  in a time varying magnetic field  $\mathbf{B}$ . With proper explanation, derive expression of induced emf and corresponding electric field. [[CO1](Remember/LOCQ)]  
 (b) A conducting bar can slide freely over two conducting rails. Evaluate the induced voltage in the bar if the bar slides at a velocity  $\mathbf{u} = 20 \hat{\mathbf{a}}_y \text{ m/s}$  and  $\mathbf{B} = 4 \cos(10^6 t - y) \hat{\mathbf{a}}_z \text{ mWb/m}^2$ . [[CO1](Evaluate/HOCQ)]



**6 + 6 = 12**

## Group - C

4. (a) In terms of  $\eta$ ,  $\beta$ ,  $\alpha$  and  $\mathbf{u}$  of plane wave, compare the propagation in free space and in lossless dielectric medium [[CO3](Remember/LOCQ)]
- (b) A lossless dielectric has an intrinsic impedance of  $200\angle 30^\circ \Omega$  at a particular frequency  $\omega$ . If, at that frequency, the plane wave propagating through the dielectric has the magnetic field component

$$\mathbf{H} = 10e^{-\alpha x} \cos\left(\omega t - \frac{1}{2}x\right) \hat{\mathbf{a}}_y \text{ A/m}$$

Find  $\mathbf{E}$  and  $\alpha$ . Determine the skin depth and wave polarization. [[CO3](Apply/HOCQ)]

**6 + 6 = 12**

5. (a) Derive Poynting's theorem. [[CO3](Remember/LOCQ)]
- (b) In a nonmagnetic medium  $\mathbf{E} = 4 \sin(2\pi \times 10^7 t - 0.8x) \hat{\mathbf{a}}_z \text{ V/m}$ . Find the time-averaged power carried by the wave. [[CO3](Analyze/IOCQ)]

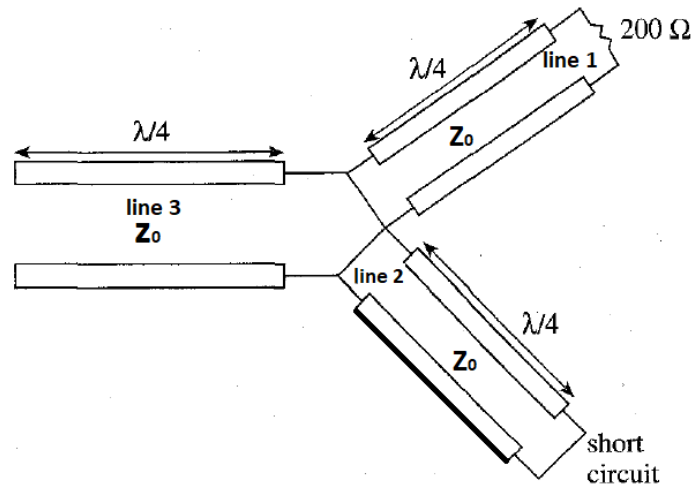
**6 + 6 = 12**

## Group - D

6. (a) Derive the characteristic impedance of a transmission line having length  $L$ . [[CO3](Analyze/IOCQ)]
- (b) A distortionless line operating at 120 MHz has  $R = 20 \Omega/\text{m}$ ,  $L = 0.3 \mu\text{H}/\text{m}$ , and  $C = 63 \text{ pF}/\text{m}$ . (a) Determine  $\gamma$ ,  $u$ , and  $Z_0$ . (b) How far will a voltage wave travel before it is reduced to 20% of its initial magnitude? [[CO3](Analyze/IOCQ)]

**6 + 6 = 12**

7. (a) Consider the three lossless lines in Figure.



If  $Z_0 = 50\Omega$ , Evaluate

- (i)  $Z_{in}$  looking into line 1  
 (ii)  $Z_{in}$  looking into line 2  
 (iii)  $Z_{in}$  looking into line 3

[[CO4](Evaluate/HOCQ)]

- (b) Find the voltage reflection coefficient at the load end for a transmission line circuit connect to a load  $Z_L$ . Assume characteristic impedance of transmission line is  $Z_0$  [[CO3](Remember/LOCQ)]

**6 + 6 = 12**

## Group - E

8. (a) A transmitting antenna has an effective aperture of  $0.5 \text{ m}^2$  and operates at 3 GHz. Calculate its directivity. [[C05](Analyse/HOCQ)]  
(b) Define a half-wave dipole antenna and describe its radiation pattern. [[C05](Remember/LOCQ)]  
(c) What is the difference between beamwidth and directivity? How does beamwidth affect antenna performance? [[C05](Apply/IOCQ)]  
**3 + 4 + 5 = 12**
9. (a) Compare and contrast a uniform and a non-uniform linear antenna array in terms of excitation, directivity, and sidelobe control. [[C06](Analyse/HOCQ)]  
(b) Explain the role of the array factor in determining the radiation pattern of a linear antenna array. [[C06](Remember/LOCQ)]  
(c) A uniform linear array consists of 5 isotropic elements spaced  $\lambda/2$  apart. Determine the array length if the operating frequency is 3 GHz. [[C06](Apply/IOCQ)]  
**4 + 4 + 4 = 12**
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Cognition Level	LOCQ	IOCQ	HOCQ
Percentage distribution	38.54	35.42	26.04